Use of Head-Tail Chromaticity Monitor for the LHC.

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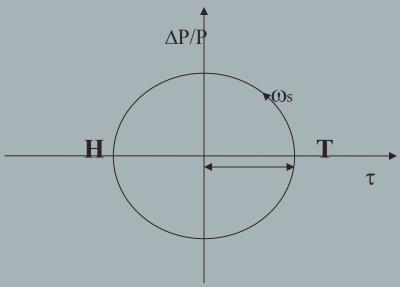


Overview

- ▲ Introduction to Head-Tail Phase Shift method to measure chromaticity
- ▲ Set-up of H-T monitor in the Tevatron
 - ▲ Limitation of system in Tevatron.
- ▲ Measurement issues in the LHC
- ▲ Other possible uses of the H-T monitor:
 - ▲ Fitting Wake fields, 2nd order Chromaticity



Longitudinal Beam Dynamics



Longitudinal 'phase-space' Graph

$$\delta(s) = \frac{-2\pi q_s}{\eta C} r \sin(2\pi q_s s / C + \varphi)$$

$$z(s) = r\cos(2\pi q_s s / C + \varphi)$$



Chromaticity Measurement Using Head-Tail Phase Shift

In the presence of non-zero chromaticity the betatron frequency is perturbed by:

$$\omega_{\beta}(\delta) = \omega_{\beta 0} + \omega_0 \xi \delta$$

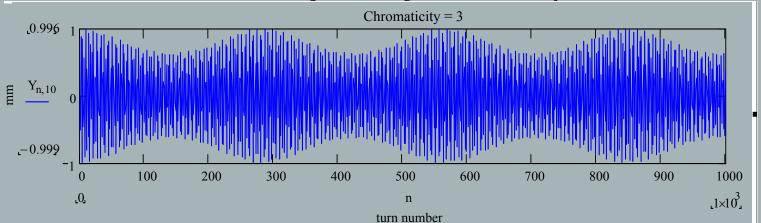
the equation of motion per particle becomes:

$$A\exp\left[\pm i(2\pi Qn + \frac{\xi\omega_0}{\eta}\tau(1-\cos(2\pi q_s n)) + \frac{\delta\xi}{q_s}\sin(2\pi q_s n))\right]$$

Which when integrated over a guassian δ distribution gives[1]:

$$Y(\xi, \tau, n) = e^{-\frac{\omega_0^2 \xi^2 \sigma_{\tau}^2}{2\eta^2} \sin^2(2\pi q_s n)} \sin \left[2\pi Q n + \frac{\omega_0 \xi}{\eta} \tau (1 - \cos(2\pi q_s n)) \right]$$

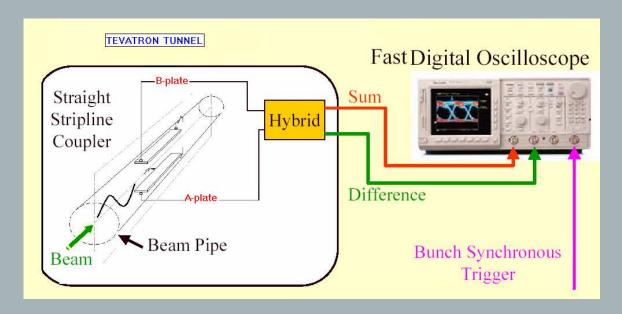
The result of this simple model predicts a beam envelope which recoheres every half synchrotron period.



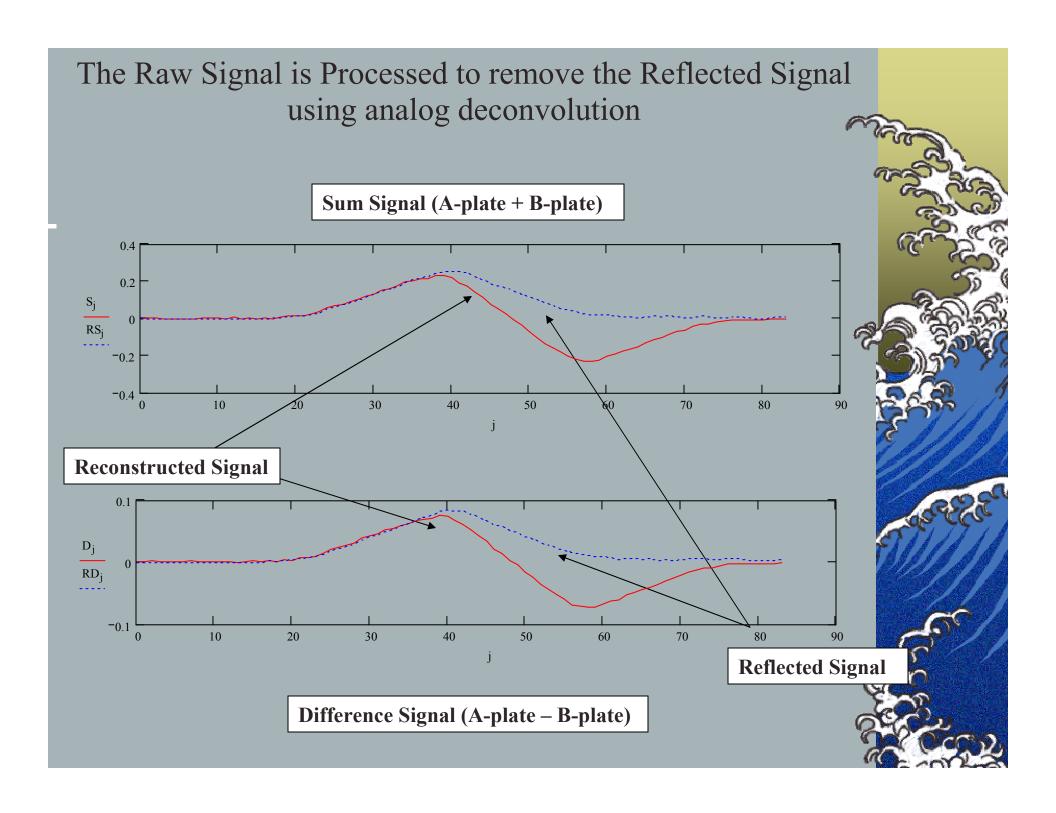
And a phase which recoheres every full synchrotron period reaching a maximum phase difference every half synchrotron period. Thus from the phase difference between two locations in a bunch the chromaticity can be calculated using:

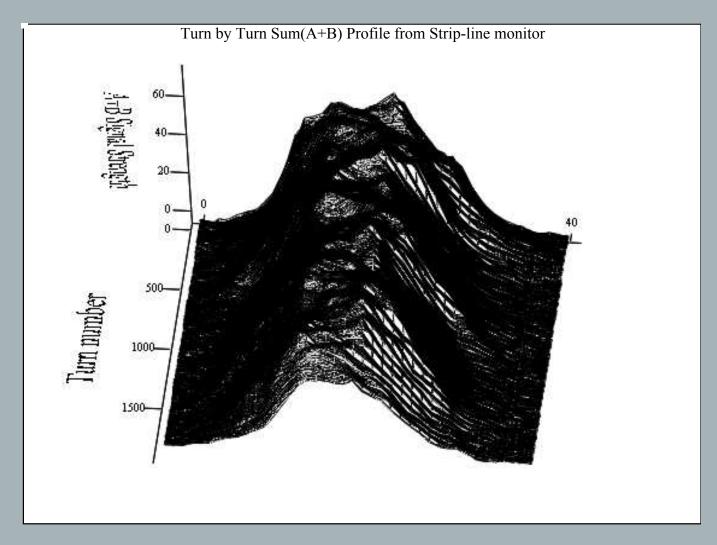
$$\xi = -\eta \frac{\Delta \Psi}{\omega_o \Delta \tau (\cos(2\pi n q_s) - 1)}$$

Extracting Transverse position



Using the vertical and horizontal strip-line detectors installed in the Tevatron at the F0 location we extract a profile of the transverse behavior of the beam over a single longitudinal bunch.





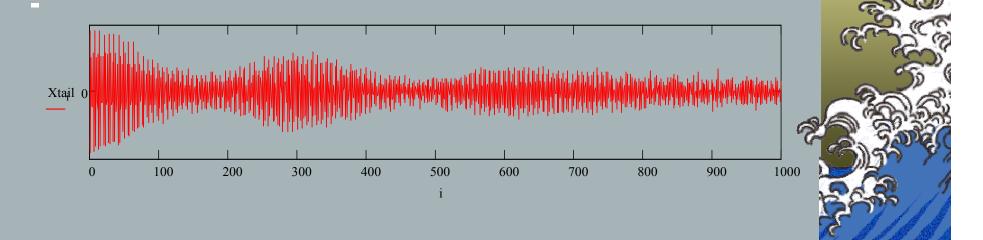


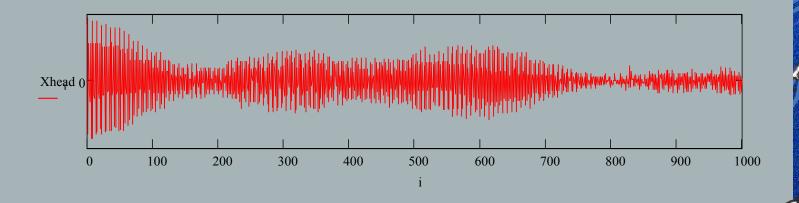
From the Sum and Difference (A-plate \pm B-plate) Signals the Transverse position can be calculated using:

$$X(n, \tau) = 27 \times G \cdot \frac{Difference(A(n, \tau) - B(n, \tau))}{Sum(A(n, \tau) + B(n, \tau))}$$

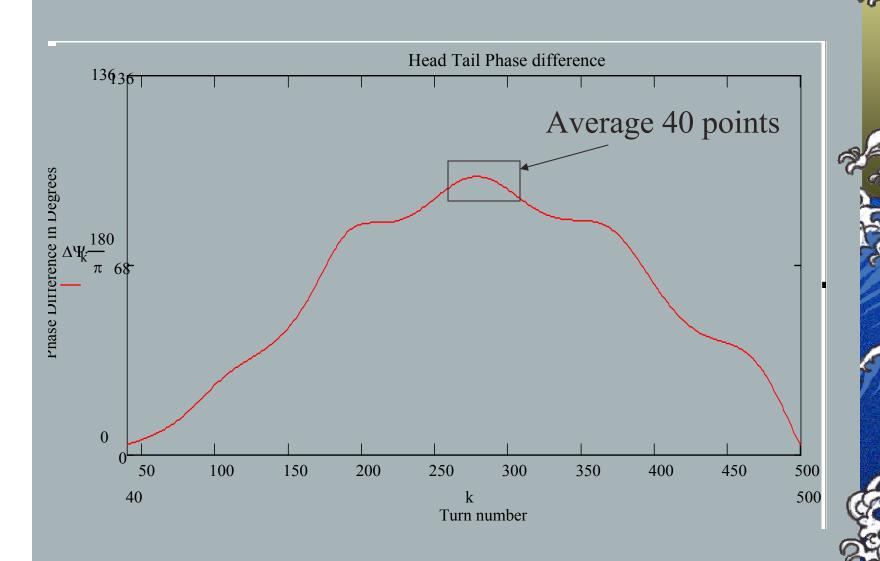
Here G is the ratio of the A-B gain over the A+B gain. Once the Transverse Position as a function of longitudinal bunch position is known (τ) we can use this to analyze the phase shift between the Head and the Tail to Calculate Chromaticity.

Vertical turn by turn position after vertical 1.6 mm kick. Head and Tail are separated by .8 nsecs



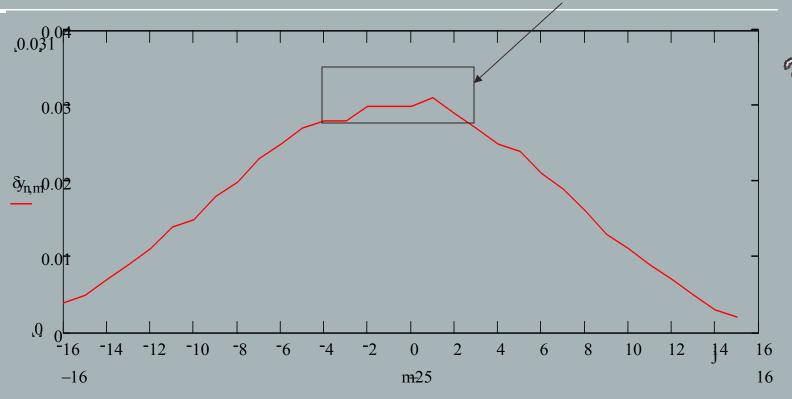


Head Tail Phase Evolution for Chromaticity = 5 units

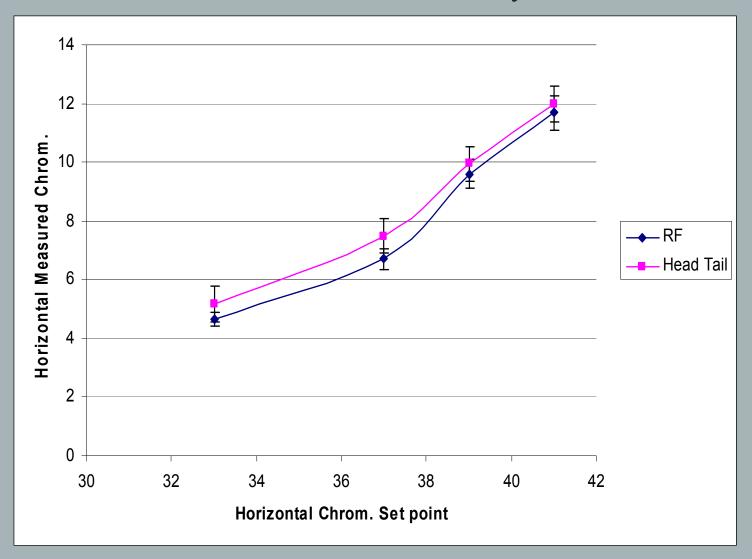


Then we take total of 7 bunch slices around the bunch center and take phase differences between head and tail points, then average them all

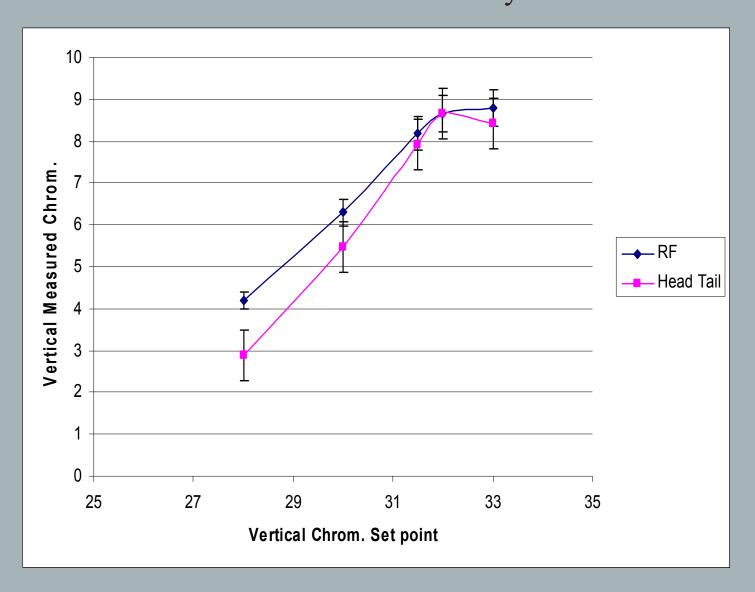
Take 3 points on either Side of bucket



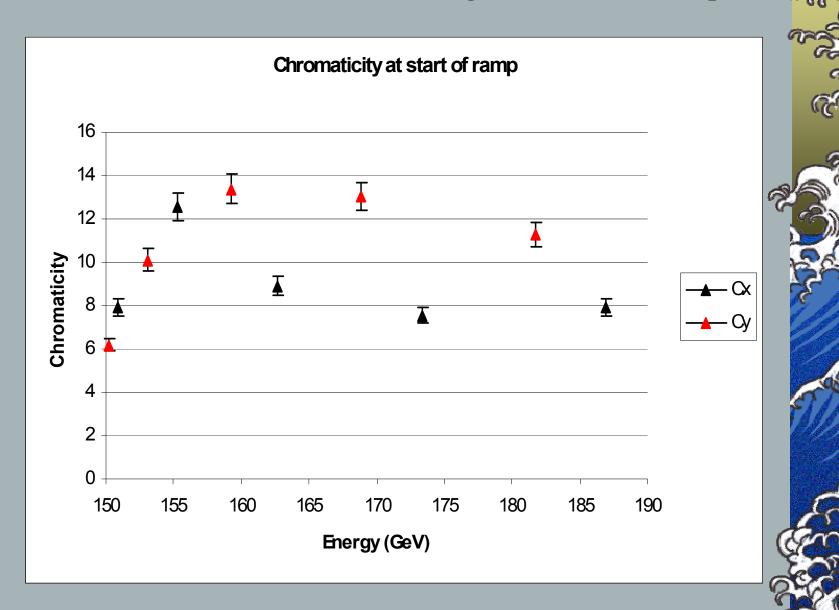
Comparison of Head-Tail with RF at 150 GeV for Horizontal Chromaticity



Comparison of Head-Tail with RF at 150 GeV for Vertical Chromaticity

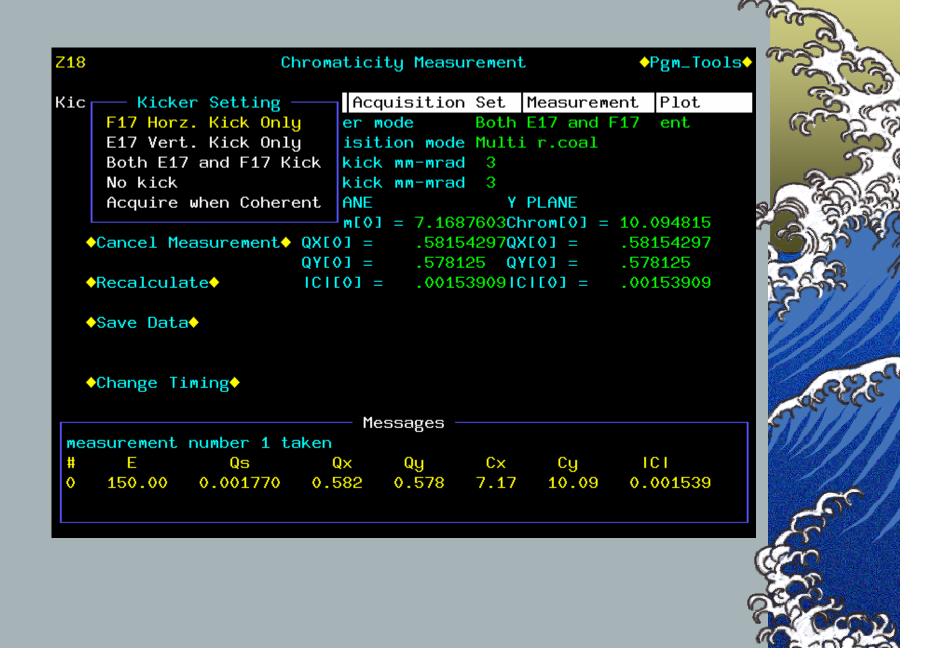


Results from test during Acceleration ramp

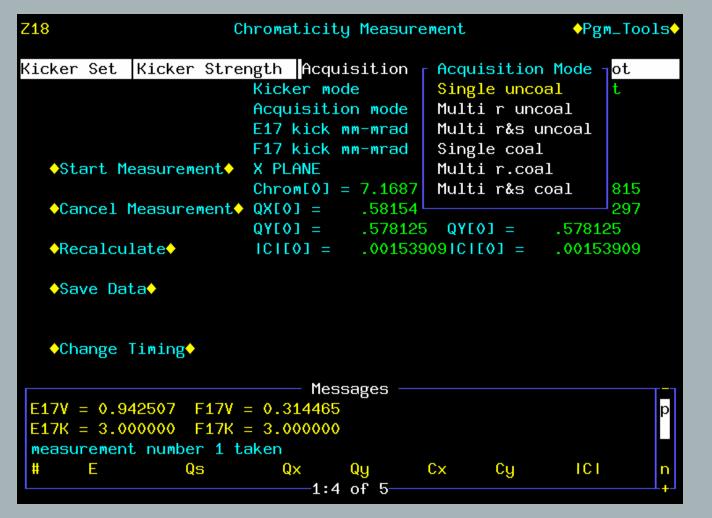


C100 Program

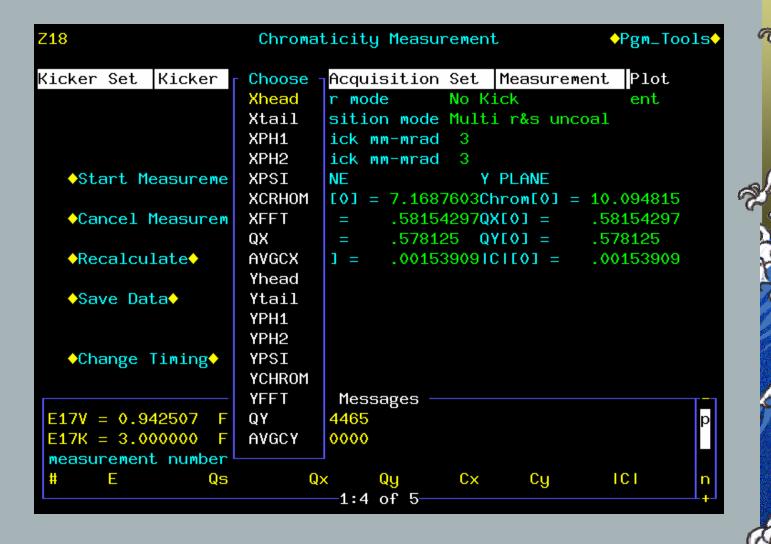
```
Z18
                                                           ◆Pgm_Tools◆
                      Chromaticity Measurement
Kicker Set | Kicker Strength | Acquisition Set | Measurement | Plot
                         Kicker mode
                                          Both E17 and F17
                                                             ent
                         Acquisition mode Multi r.coal
                         E17 kick mm-mrad 3
                         F17 kick mm-mrad 3
   ◆Start Measurement◆ X PLANE
                                              Y PLANE
                         Chrom[0] = 7.1687603Chrom[0] = 10.094815
   ◆Cancel Measurement◆ QX[0] =
                                    .58154297QX[0] = .58154297
                         QY[0] = .578125 \quad QY[0] = .578125
   ◆Recalculate◆
                         |C|[0]| =
                                    .00153909[CI[0] =
                                                         .00153909
   ◆Save Data◆
   ◆Change Timing◆
                               Messages
 measurement number 1 taken
                                                           ICI
                                                   Cy
                 Qs
                            \mathbf{Q}\mathbf{x}
                                   Qy
                                           \mathsf{C}\mathsf{x}
     150.00
              0.001770
                          0.582
                                  0.578
                                           7.17
                                                  10.09
                                                          0.001539
```

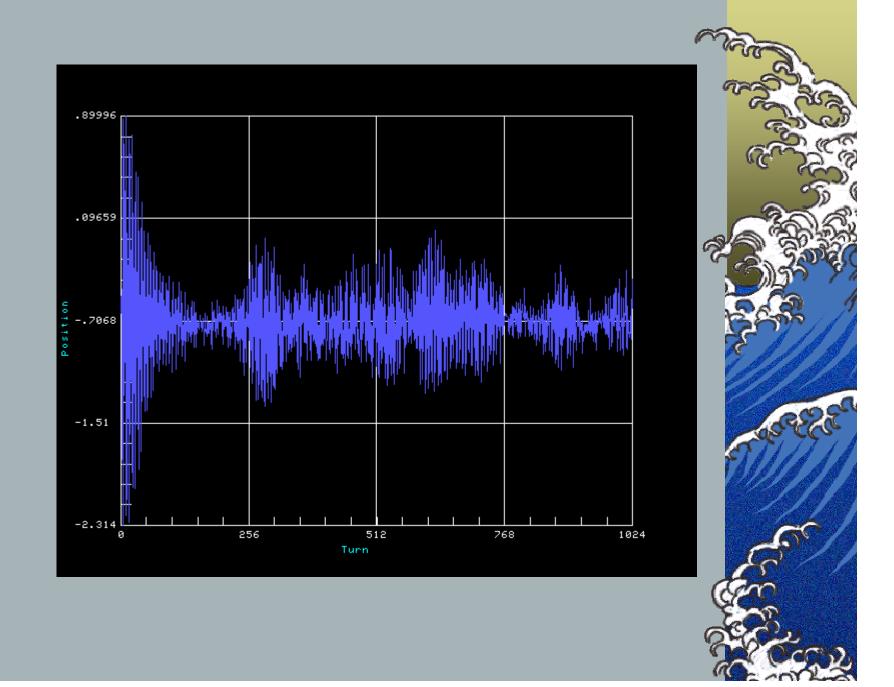


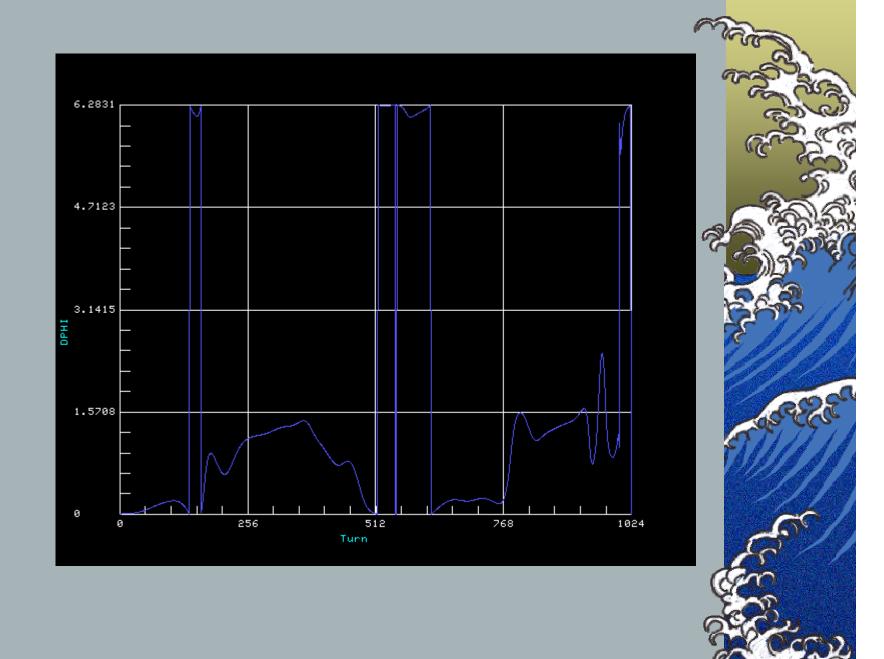
```
◆Pgm_Tools◆
Z18
                   Chromaticity Measurement
Kicker Set Kicker Strength Settings at 150 GeV -
                    E17 vert.kick [3 ]
                                            mm-mrad pi
                    F17 horz, kick [3 ]
                                             mm-mrad p
                                 -Return-
                     F17 kick mm-mrad 3
  ◆Start Measurement◆ X PLANE
                                      Y PLANE
                     Chrom[0] = 7.1687603Chrom[0] = 10.094815
  ◆Cancel Measurement◆ QX[0] = .58154297QX[0] =
                                                .58154297
                     QY[0] = .578125 QY[0] = .578125
  .00153909
  ◆Save Data◆
  ◆Change Timing◆
                        Messages
 measurement number 1 taken
                                                  ICI
              Qs
                       \mathbf{Q}\mathbf{x}
                             Qy
                                    \mathsf{C}\mathsf{x}
                                          Cy
    150.00
            0.001770
                             0.578
                     0.582
                                    7.17
                                          10.09
                                                 0.001539
```

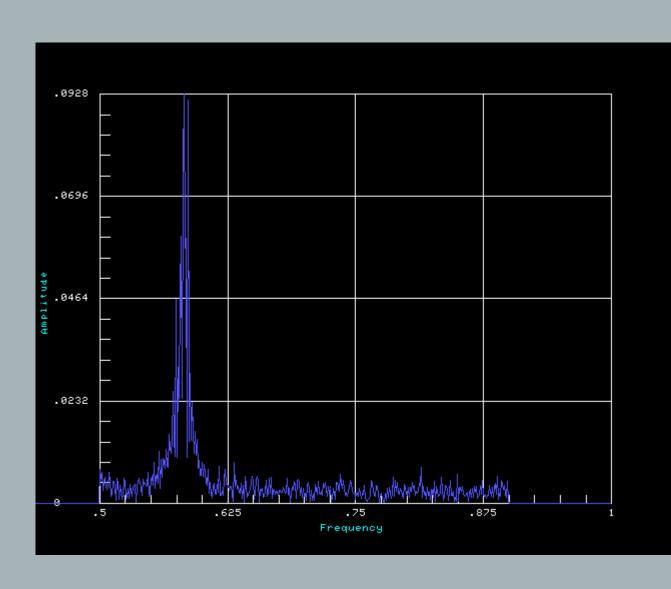


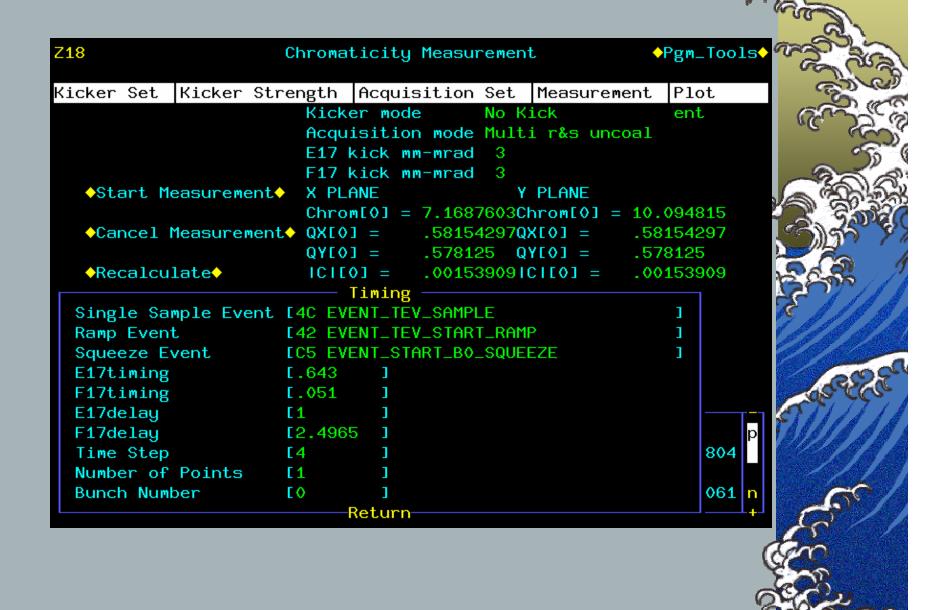












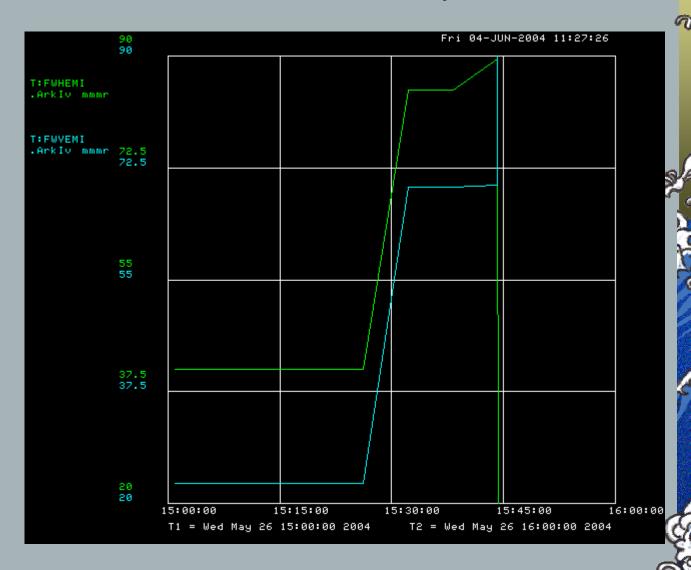
Limitations of current set-up

- ▲ Destructive measurements
 - ▲ Emittance blow up, aperture limitations
- ightharpoonup Tracking Phase over 2π
- ▲ Extracting usable signal
 - ▲ *Phase contamination: coupling*
 - ▲ Decoherence time: Tune spread
 - **▲** Linear chrom.
 - ▲ 2nd order chrom
 - **▲** Octupoles
 - **▲** Impedance
 - **▲** beam intensity

 - ▲ *synchrotron tune.*



Emittance Blow up after 5 kicks in Horizontal and 5 kicks vertically

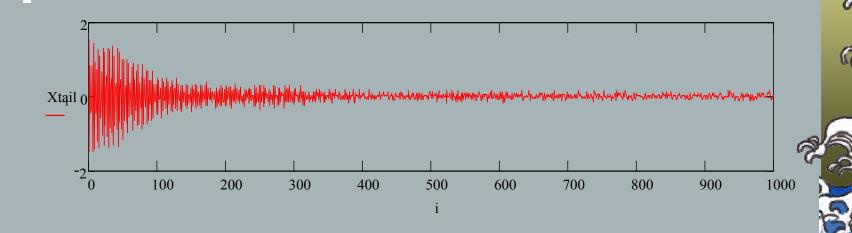


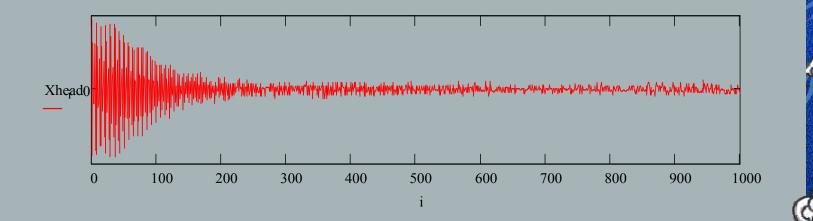
Decoherence time

- •Octupoles at Injection:
 - •Damping time can be less than 100 turns
 - Effected by
 - •bunch intensity (need > 280E+9) to get signal at 300 turns.
 - transverse emittance.
- Flat-top
 - high chromaticities
 - longer synchrotron periods

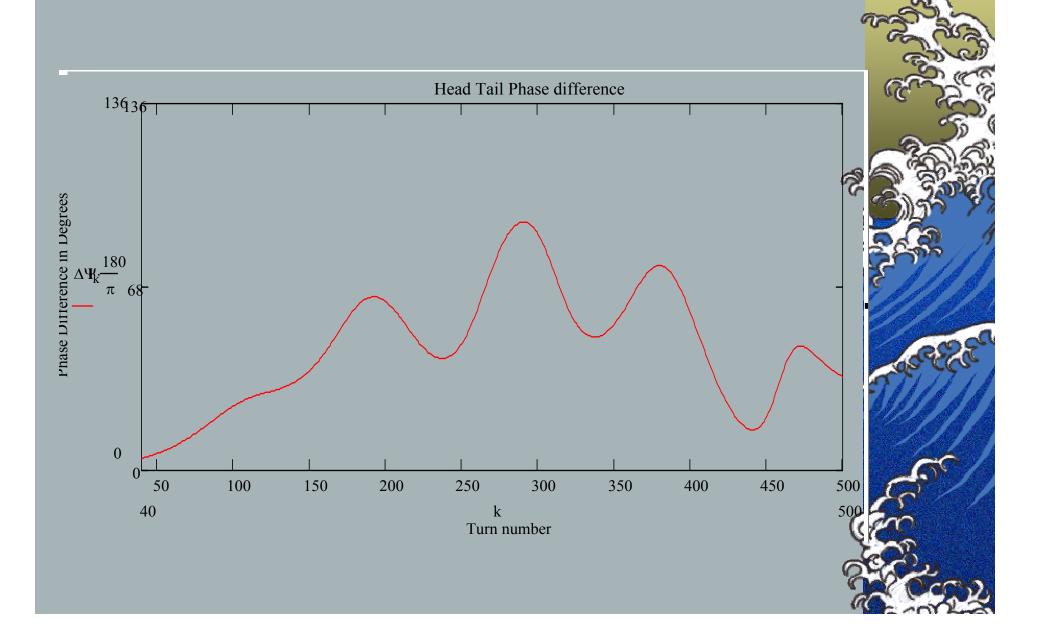


Head and Tail turn-by-turn vertical motion with strong Coupling and Octupoles on.





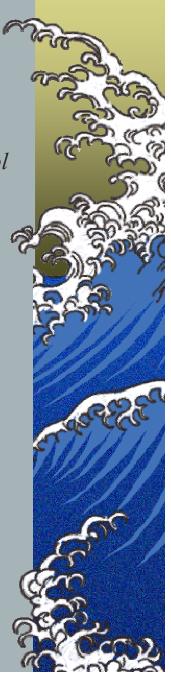
Less usable signal with faster decoherence time.



LHC and Tev Parameters[2]

	Tev Injection	Tev Flattop	LHC Injection	LHC Flattop
Energy (GeV)	150	980	450	7000
Revolution Frequency (kHz)	47.7		11.245	
Synchrotron Frequency (Hz)	86	34	61.8	21.4
rms bunch length (nsec)	3	1.7	.37	.25
Slip factor	.0028		.0003	
Bunch Intensity	3e11		1e11	
Aperture (mm)	74		44	

- ▲ *Synchrotron Period:*
 - ▲ 182 525 turns in LHC
 - ▲ 564 1412 turns in Tev
- ▲ Chromaticity Range &
 - ▲ (2 to +/-50 units) in LHC initially later (+/- 15 units) need control to 0.5 units tolerance 5 units [3]
 - ▲ (0 to 25 units) in Tev
- △ 2nd Order Chromaticity Range ξ2
 - ▲ 11,000 uncorrected in LHC [3]
 - ▲ ~1500 in Tev
- ▲ Damping Time (LHC) [3]
 - ▲ 8 turns at 50 units of Chrom, 130 turns at 10 units.
 - ▲ 250 turns at collisions
- ▲ Maximum Chrom. Measurement (0 to 2π)
 - ▲ In Tevatron we reach our maximum for a two point measurement at 2.5 GHz at 20 units
 - ▲ *In the LHC this will be 15 units at 2.5 GHz.*
- △ Coupling at injection: |C-| = 0.01, FT 0.001[3]



Measurement Issues in LHC

- ▲ Larger swings in Chromaticity in the LHC
 - ▲ (> 50 unit swing during 30 sec snap back with only 80% control from feed forward). [4]
- ▲ Decoherence Time
 - ▲ High 2nd order chromaticity
 - ▲ Helped by a shorter synchrotron period..
 - ▲ With Chrom > 20 units becomes a problem
- *▲ Emittance blow-up*
 - ▲ Use current current method of kicking beam ~ 1 mm will allow only ~ 10 kicks.
- ▲ Longitudinal Bunch Motion?
 - ▲ This currently makes HT measurements in Tevatron with uncoalesced bunches very difficult.

Possible Solutions and Plans for HT use in the LHC

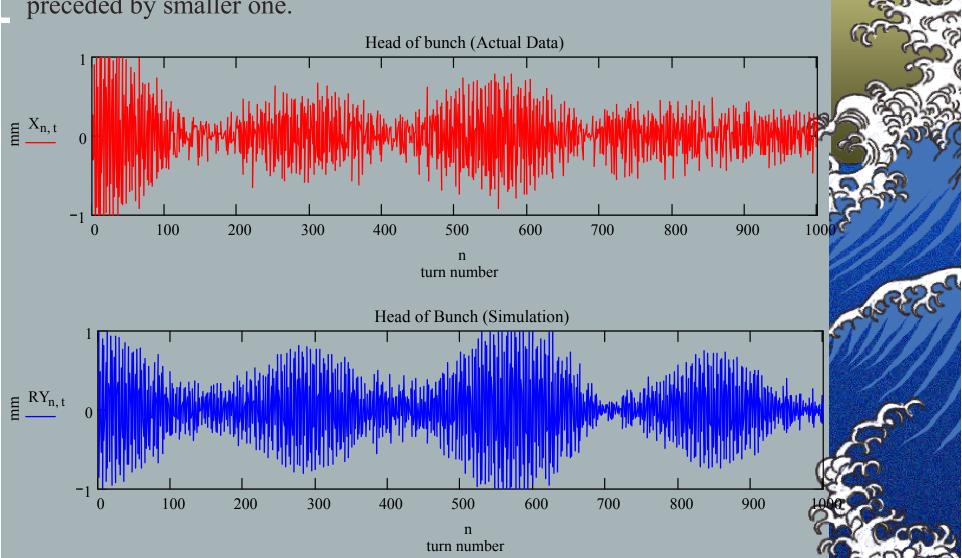
- ▲ Large Chromaticities
 - ▲ damping time
 - ▲ *Tracking phases* > 360 degrees
 - ▲ Solution: Measure damping time or frequency width to grossly estimate large chromaticities.
- ▲ Damping Time and Emittance Blow up
 - ▲ Solution: Improve S/N by taking out the closed orbit offset in the signal
 - ▲ *Auto-zeroing using variable attenuators*
 - ▲ Using diodes: CERN guys now propose using a two diode system to measure top and bottom of doublet. To be tested in SPS next summer. (Perhaps we can try it now in the Tev?)
- ▲ The current plan for HT in LHC
 - ▲ Still in flux
 - \blacktriangle *Use PLL method for Q and Q'?*
 - ▲ Maybe be important for snap-back since it is possible to extract 10 measurements with tolerable beam blow-up.[3]

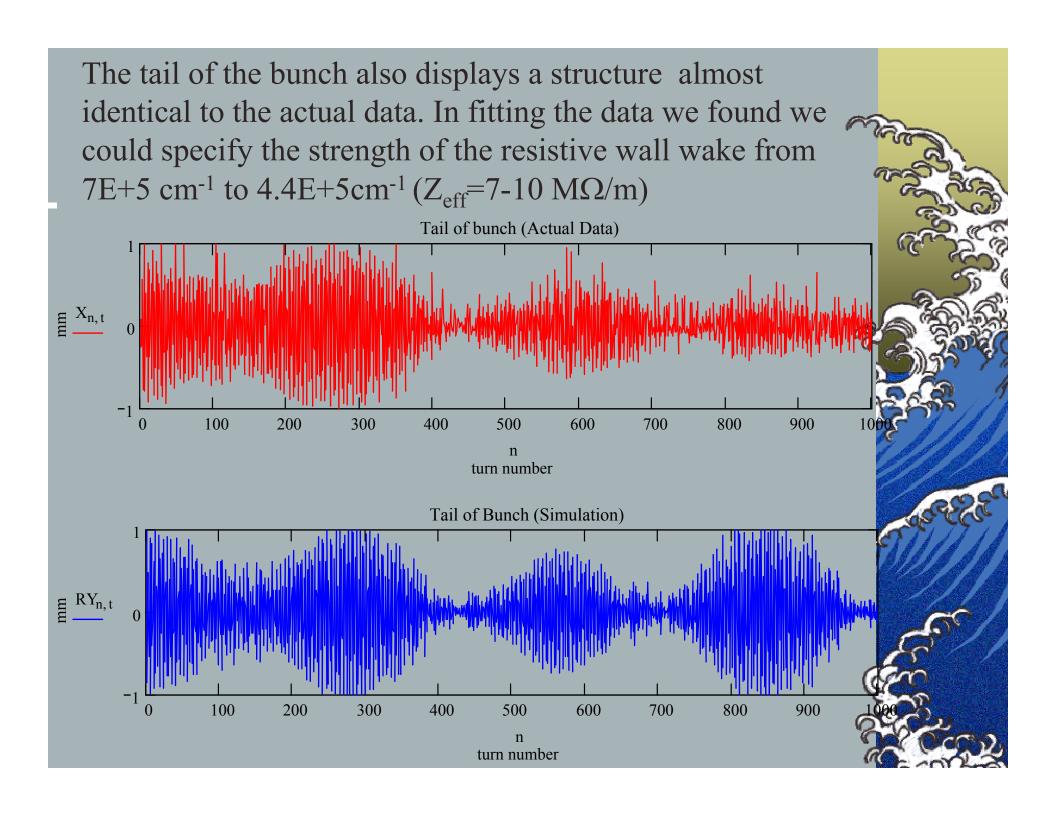
Other Possible Measurements with HT monitor

- ▲ Measure Wake field strength?
- *▲ Measure 2nd Order Chromaticity?*
 - ▲ Evolution of Beam Envelope over Bunch
 - ▲ Compare with multiparticle simulations

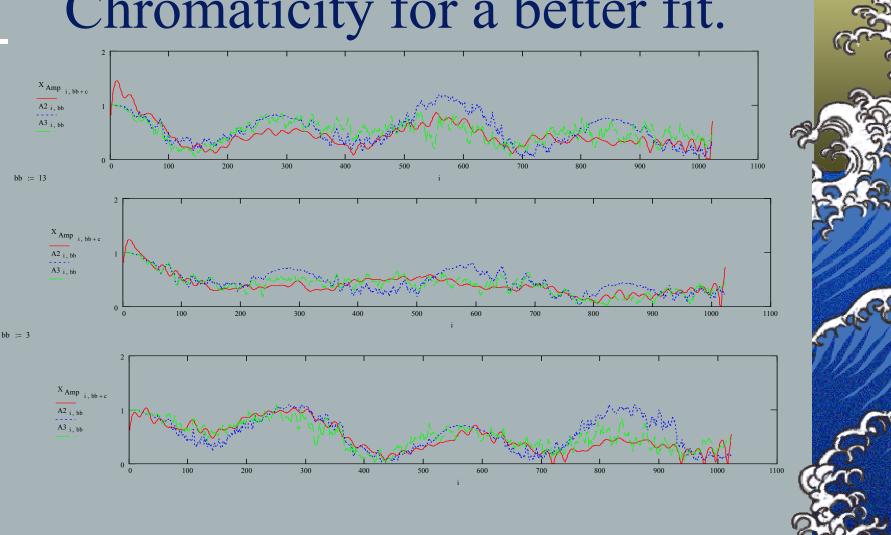


The Results of multi-particle simulation N=1000 particles with Resistive wall wake field 4.4E+5cm⁻¹ (Z_{eff} =7 M Ω /m) ξ =3.733 total charge equal 2.6E+11 e . We did not include 2nd order chromaticity. The behavior is almost identical. Especially you can see larger re-coherence followed preceded by smaller one.





Now adding 2nd Order Chromaticity for a better fit.



Conclusion

- ▲ Applying the HT Chromaticity in LHC will involve overcoming several issues
 - **▲** *Emittance blow-up*
 - ▲ Decoherence time
 - ▲ Tracking large Chromaticity swings
 - ▲ Coupling issues
 - ▲ Perhaps issues with longitudinal bunch motion?
- ▲ The information we get from the HT monitor can be mined to extract in addition to linear chromaticity, wake field strength, 2nd Order chromaticity and perhaps other effects at this stage these fits must be done offline but with more experience and perhaps using empirical model based on simulation.



References:

- [1] S. Fartoukh and R. Jones, LHC Project Report 602
- [2] LHC Beam parameters and definitions (Vol 1. Chapter 2.)
- [3] S. Fartoukh and J.P. Koutchouk,, LHC-B-ES-0004 rev 2.0 (2004)
- [4] R. Jones, Beam measurement capabilities for controlling dynamic effects in the LHC (LHC Reference Magnetic System Review July 27th and 28th 2004)

